GCE

## Mathematics

Advanced GCE

## Unit 4734: Probability and Statistics 3

## Mark Scheme for June 2011

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Mark schemes should be read in conjunction with the published question papers and the Report on the Examination.

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| 1 (i) | $\begin{aligned} & \mathrm{E}(S)=22 \\ & \operatorname{Var}(S)=\mathrm{E}(S) \end{aligned}$ | $\begin{array}{ll} \hline \text { B1 } & \\ \text { B1 } & 2 \end{array}$ |  |
| :---: | :---: | :---: | :---: |
| (ii) | $\begin{aligned} \mathrm{E}(T) & =1 / 1 \times 5-1 / 4 \times 4=1.5 \\ \operatorname{Var}(T) & =1 / 4 \times 5+1 / 1 \times 4 \\ & =1.5=\mathrm{E}(T) \mathrm{AG} \end{aligned}$ | $\begin{array}{ll} \text { B1 } & \\ \text { M1 } & \\ \text { A1 } & 3 \end{array}$ | Using $\operatorname{Var}(a X+b Y)$ CWO |
| (iii) | $T$ only does not have a Poisson distribution Some values of $T$ are EITHER negative OR: fractional | $\begin{array}{lr} \text { B1 } & \\ & \\ & \text { B1 } \\ & 2 \\ & (7) \\ \hline \end{array}$ | Unless wrong reason |
| 2(i) | $\begin{aligned} & \text { Use }(6 / 80)(74 / 80) / 80 \\ & p_{\text {s }} \pm z s \\ & z=1.96 \\ & (0.0173,0.1327) \end{aligned}$ | $\begin{array}{ll}\text { B1 } & \\ \text { M1 } & \\ \text { B1 } & \\ \text { A1 } & 4\end{array}$ | Or /79 $s$ of the form $\sqrt{ }\left(p_{s} q_{s} / 80\right)$ (or 79) or no $\sqrt{ }$ Accept (0.017,0.133) |
| (ii) | $\begin{aligned} & \text { Use } \mathrm{z} \sqrt{ }\left(p_{s} q_{s} / n\right) \\ & \leq 0.05 \\ & n \geq 106.6 \text {, least is } 107 \end{aligned}$ | M1 <br> A1 <br> A1 3 | $\begin{aligned} & \text { or no } V \\ & \text { and } \mathrm{z}=1.96 \text {.Or }= \end{aligned}$ <br> Allow 110 |
| (iii) | e.g Variance is an estimate OR Distribution of $p_{s}$ is only approx normal | $\begin{array}{\|lr} \hline \text { B1 } & \mathbf{1} \\ & (\mathbf{8}) \\ \hline \end{array}$ | Not var unknown <br> Must state distribution of what. |
| 3(i) | $\begin{aligned} & \int_{0}^{1} a x d x+\int_{1}^{2} a(x-2)^{2} \mathrm{dx}=1 \\ & {\left[\frac{a x^{2}}{2}\right]_{0}^{1}+\left[\frac{a(x-2)^{3}}{3}\right]_{1}^{2}} \\ & 1 / 2 a+1 / 3 a=1 \\ & \quad a=6 / 5 \end{aligned}$ | $\begin{array}{ll} \text { M1 } & \\ \text { B1 } & \\ & \\ \text { M1 } & \\ \text { A1 } & 4 \end{array}$ | With or without limits <br> Correct method for equation with fractions/decimals |
| (ii) | $\begin{aligned} & \text { EITHER: } \int_{0}^{1} a x \mathrm{~d} x+\int_{1}^{1.5} a(x-2)^{2} \mathrm{~d} x \\ & \text { OR } 1-\int_{1.5}^{2} a(x-2)^{2} \mathrm{~d} x \\ & ={ }^{19} / 20 \end{aligned}$ | M1 <br> A1 2 | Any $a$ AEF |
| (iii) | $\begin{aligned} & \int_{0}^{1} a x^{2} \mathrm{dx}+\int_{1}^{2} a x(x-2)^{2} \mathrm{dx} \\ & =\left[\frac{a x^{3}}{3}\right]_{0}^{1}+\left[a\left(\frac{x^{4}}{4}-\frac{4 x^{3}}{3}+2 x^{2}\right]_{1}^{2}\right. \end{aligned}$ | M1 <br> B1 | AEF With or without limits |
|  | =9/10 <br> (Expected monthly demand $=900$ ) | $\begin{array}{lr} \text { A1 } & 3 \\ & (9) \end{array}$ | AEF |




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